

## Statistics Terminology for Hypothesis Testing

$p\text{-value} \leq \alpha \Leftrightarrow$  statistically significant  $\Leftrightarrow$  reject  $H_0$  (i.e., accept  $H_1$ ) [*possible* Type I error]  
 $p\text{-value} > \alpha \Leftrightarrow$  not statistically significant  $\Leftrightarrow$  fail to reject  $H_0$  (i.e., accept  $H_0$ ) [*possible* Type II error]

$\alpha$  = probability of a type I error = significance level

$\alpha$  is measured on the  $H_0$  distribution (or frequency plot) from the critical value (the decision rule cutoff value) in the direction of extreme (see the other side of this page).

$\beta$  = probability of a type II error

$\beta$  is measured on the  $H_1$  distribution (or frequency plot) from the critical value (the decision rule cutoff value) in the opposite direction from the direction of extreme (see the other side of this page).

p-value = probability of the given observation or one more extreme, *assuming  $H_0$  is true*.

p-value is measured on the  $H_0$  distribution (or frequency plot) from the observed value in the direction of extreme.

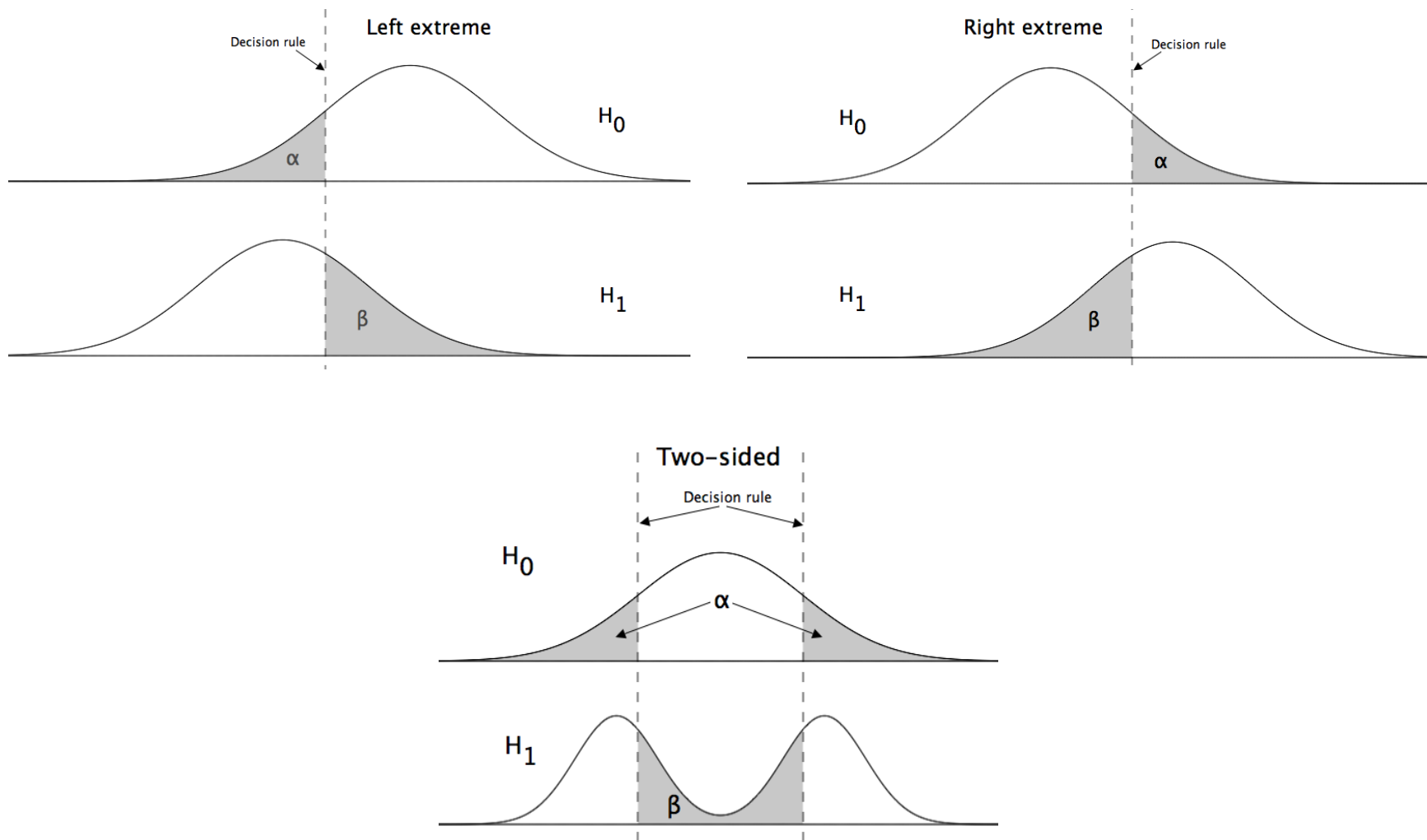
A larger p-value supports  $H_0$ ; a smaller p-value supports  $H_1$  (as compared with  $\alpha$ ).

(Remember that you must have made an observation – taken a sample, etc. – before you can have a p-value.)

Type I error means rejecting  $H_0$  (i.e., accepting  $H_1$ ) when  $H_0$  is actually true.

Type II error means failing to reject  $H_0$  (i.e., accepting  $H_0$ ) when  $H_0$  is actually false.

		---- reality ----	
		$H_0$ is true	$H_1$ is true
your conclusion	<b>Accept <math>H_0</math></b> (“fail to reject $H_0$ .”)	No error	Type II error
	<b>Accept <math>H_1</math></b> (“reject $H_0$ .”)	Type I error	No error



The horizontal scales of the  $H_0$  and  $H_1$  distributions must align.

p-value is measured similarly to  $\alpha$ , but starting from the observation instead of from the decision rule. In the two-sided case, you must also include the equivalently extreme value on the opposite side from the observation (or just double the p-value from one side).